# The MIRAGE-e model (Version 1.1)

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### A note on the MIRAGE model family

- Several institutions use "MIRAGE" in the MIRAGE consortium and some of them developed their own variants of the model.
  - CEPII, IFPRI, EU Commission, INRA, ITC Geneva, UNECA
  - Coordinated by the CEPII, and open for free to new members
- MIRAGE-e is a proposal by CEPII to keep MIRAGE core assumptions while follow GTAP updates closely, dealing with energy issues, and using a refined baseline. It is meant to be:
  - provided to all consortium members
  - dedicated to be opensource
- This presentation corresponds to MIRAGE-e version 1.1 beta (1.1 to be released soon).
- More information available at http://wiki.mirage-model.eu.





Model structure

### Databases I

- **GTAP database** version 9.2, 2011 base year
- Tariffs and NTMs
  - MAcMap HS-6 Tariffs aggregated to GTAP and model level by the reference group method

http://www.cepii.fr/CEPII/en/bdd\_modele/presentation.asp?id=12

■ **AVE of NTMs** in goods – Ad-valorem equivalents (AVEs) of non-tariff measures by Kee, Nicita and Olarreaga (2009)

http://go.worldbank.org/FG1KHXSP30

■ **AVEs-Services** – AVEs for NTMs in services by Fontagné et al. (2016)

http://www.cepii.fr/CEPII/en/bdd\_modele/presentation.asp?id=33

■ Value of Time – AVEs by Minor (2013), after Hummels and Schaur (2013)

https://impactecon.com/resources/data/



#### Databases II

- Baseline data
  - **EconMap** Baseline projections for GDP, factors, productivity, etc., version 2.4

http://www.cepii.fr/CEPII/en/bdd\_modele/presentation.asp?id=11

- Other
  - USDA Commodity and Food Elasticities Used to calibrate LES-CES demand

https://www.ers.usda.gov/data-products/commodity-and-food-elasticities/

- New commodities
  - None.



#### Production structure I

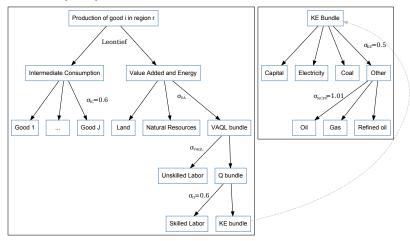
- Leontief between value-added and intermediate consumption
- Two cases: Energy in value-added (EVA) or Energy as intermediate consumption; depending on the chosen aggregation of energy sectors .
  - EVA case only: three archetypes refined petroleum, other fossil fuels, other
  - Otherwise: One standard archetype ("Non-EVA", standard in former versions of MIRAGE)
- Capital vintage
  - Putty-clay: Old capital is immobile, new capital perfectly mobile
- Market structure:
  - Perfect competition with constant return to scale
  - or Imperfect competition à la Krugman with increasing returns to scale



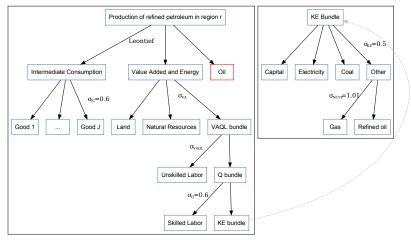
### Production structure II

- EVA case only: Energy
  - Energy substitutes with capital
  - Deeply nested energy bundle
- EVA case only: Consistency in physical volume (Mtoe, MtCO<sub>2</sub>)
  - $\blacksquare$  Production in volume is  $\propto$  physical quantity
  - Two endogenous coefficients guarantee that, in physical quantities,
    - Production = Local demand + Foreign demand
    - Households consumption + Intermediate consumption =
      Demand for local good + Demand for foreign good

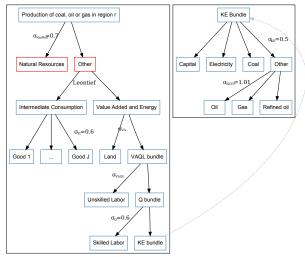
#### Standard (EVA) nesting:



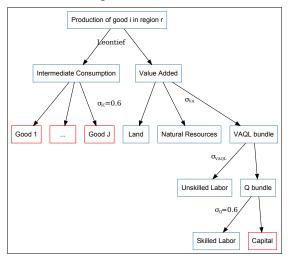
#### Refined petroleum production (EVA) nesting:



### Primary fossil fuel production (EVA) nesting:



#### Non-EVA nesting:





# Typical elasticities

Symbol	Elasticity	Value
$\sigma_{IC}$	Intermediate consumptions	0.6
$\sigma_{V\!A}$	Land – Natural Resources – VAQL	1.01 // 0.1
$\sigma_{V\!AQL}$	Unskilled Labor – Q	ESUBVA
$\sigma_{Q}$	Skilled Labor – KE	0.6
$\sigma_{\it KE}$	Capital – Electricity – Coal – Other	0.5
$\sigma_{\it NCFF}$	Oil – Gas – Refined oil	1.01



# Output disposition

Homogenous output (products are not differenciated by destination)



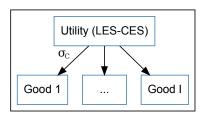
### Income distribution

- Representative agent gathering housholds and government
  - Collects tax revenue directly.
  - Equivalent to a non-distorsive lump-sum transfert.



### Final demand

- Exogenous share of disposable income is saved
- Single level LES-CES specification (both households and government)
  - Elasticity and minimal consumption calibrated to match USDA price and income elasticities



#### Factor markets I

- Labor:
  - Perfect mobility between sectors, labor immobile between regions
  - Agricultural vs. non-agricultural segmentation to be updated
- Capital:
  - Installed capital immobile (depreciation à 6%)
  - New capital perfectly mobile between sectors
    - Level of new capital by region determined by domestic savings
      + current account balance
    - Allocation between sectors based on return to capital ( $\alpha = 40$  is the elasticity of investment to return to capital)

$$INV_{i,r,s} = B_r a_{i,r,s} Capital_{i,s} e^{\alpha W_{i,s}^{Capital} / P_{s,t}^{INVTOT} - \delta_r}$$



#### Factor markets II

#### Land:

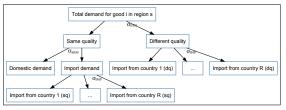
- Total (agricultural) land is an isoelastic function of the real return to land
- Regions can be "land-constrained" (elasticity 0.25) or not (elasticity 1), following the LINKAGE model specification
- Imperfect mobility between sectors (CET, elasticity 0.5)

#### Natural resources:

- Immobile.
- Constant for sectors other than primary fossil energy
- Calibrated in the baseline (see below) for primary fossil energy

#### Trade I

- Standard: Nationally nested Armington
  - D vs. M, M allocated across source regions
- Optional: Quality differentiation by region
  - Goods from the same quality-group are more substitutable



- Elasticities
  - $\sigma_{IMP} = \text{ESUBM from the GTAP database}$
  - Consistency between elasticities is obtained by the " $\sqrt{2}$ " rule:  $\sigma_{low} 1 = \sqrt{2} \left( \sigma_{high} 1 \right)$

#### Trade II

- NTMs can either be:
  - Iceberg trade cost
  - Export-tax equivalent (rent-generating)
  - Import-tax equivalent (rent-generating)
  - Any split between the 3 alternatives
  - By default: 1/3, 1/3, 1/3
- Purchasing of international transportation services
  - International transport demand is ad-volumen, aggregated at world level
  - Split by mode (depending on aggregation) and region using two Cobb-Douglas specifications

#### Market closure

- Each sector can be considered as:
  - Perfect competition: one representative firm by sector-region
  - Imperfect competition: Krugman (1980) specification [updated in 1.1, to be released soon]
    - Firms produce imperfectly substitutable varieties
    - with increasing returns to scale (elasticity following the " $\sqrt{2}$ " rule)
    - Firms consider themselves atomic: the markup is constant.
    - Hence, the actual number of firms do not matter.



## Other Balance of Payments

- Capital account
  - Capital account is exogenous (in dynamics, exogenous percentage of world GDP, see below)

### Closure

- Default closure
  - Exogenous savings rate (varies over time)
  - Exogenous current account imbalances
- Implications
  - Savings-led investment
  - Endogenous real exchange rate determined by current account imbalance
- Numeraire
  - Implicit numeraire, ensures no world inflation (World GDP in volume equals world GDP in value)

### Other features

- Kyoto greenhouse gases
  - CO<sub>2</sub> from GTAP
- Carbon policy options
  - Carbon tax
  - Cap and trade
  - Border carbon adjustment (foreign intensity, direct or indirect emissions)



Baseline features

### Baseline inputs

- Macro: the **EconMap** database (1980-2100)
  - One reference scenario plus 5 SSP scenarios, country-level (x167)
  - The database provides to MIRAGE-e, for the period 2011-2100:
    - GDP
    - Population (sourced from U.N. Population Division, or IIASA; migrations are also configurable)
    - Active population by skill level
    - Savings rate, investment rate and current account
    - Energy productivity
- Sector-specific information:
  - Coal, oil and gas price trajectories (IEA World Energy Outlook 2016 for 2011-2040 ; continued trend 2041-2100)
  - Agricultural productivity (inhouse DEA analysis): trajectories for 9 world regions and two sector groups (Crops and Livestock)

# Baseline assumptions – EconMap

- EconMap is built at CEPII along with MIRAGE-e, preserving consistency (common data sources, capital depletion, skill levels)
- It is the output of the Macroeconomics of the Global Economy (MaGE) model, with the following assumptions (in a nutshell):
  - CES aggregated production function with capital, labor and energy
  - Population from U.N. Population Division
  - Convergence of education level to best-performing countries
  - Participation rate of women depend on education
  - Savings follow a life-cycle relation to population age groups
  - Investment related to savings through a Feldstein-Horioka relation
  - TFP conditionnal convergence on education
  - Energy productivity conditional convergence on GDP per capita
- Both MaGE model and EconMap database available opensource on http://www.cepii.fr

#### CLFII

### Baseline assumptions

#### Labor

 Skilled and unskilled labor growth rates projected by EconMap (tertiary education vs. less than tertiary)

#### Capital

■ Depletion at  $\delta = 0.06$  and investment depending on savings and current account, projected by EconMap.

#### Land

No specific dynamic assumptions (follow supply curve)

#### Natural resources

- Forestry, Fishery, Other Minerals: no specific assumptions
- Coal, Oil, Gas: Natural resources calibrated to match average world price projected by the WEO. Natural resource depletion is homogenous across the world.

#### Inter-regional

 Current account trajectories projected by EconMap embody net international capital flows

# External coupling

- Natural resources 'loosely' coupled with World Energy Outlook 2016
  - Coal, crude oil and gas world prices are taken from WEO
  - Natural resources adjust endogeneously in the baseline to match price targets
  - Basic check that baseline GDP growth is not too far from WEO assumptions
- First investigations on coupling MaGE/EconMap with an energy-oriented model (POLES) to insure full consistency (technically feasible, but more work necessary)

## Policy assumptions I

- Baseline policy assumptions are specific to each paper or study. They often include:
  - Already signed FTAs between relevant countries (tariff, and/or NTMs)
  - Completion of the Single European Market (tariff, and sometimes NTM reductions)
- (Standard) 1-step baseline (TFP calibrated to match GDP level at the same time as baseline policy changes)
  - e.g. completion of the Single European Market, FTAs
- (Optional) 2-step baseline: required when baseline policy options impact significatly GDP level
  - e.g. Paris Agreement NDCs, or in the SSP scenarios: large variation in tariffs (SSP 2,3,5), transaction costs (SSP 3,5) or agricultural productivity (SSP 3,4,5)



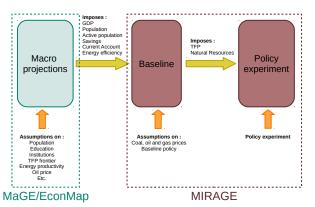
## Policy assumptions II

- 2-step baseline methodology:
  - Baseline step 1: TFP and Natural Resources calibrated to match EconMap GDPs and WEO energy prices (no other policy assumption)
  - Baseline step 2: GDP is free, implementation of the "big" policy assumptions
  - 3 Policy experiment: Compared to baseline step 2.



# Policy assumptions I

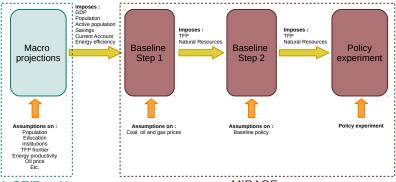
#### (Standard) 1-step baseline





# Policy assumptions II

#### (Optional) 2-step baseline



MaGE/EconMap

**MIRAGE** 



## Productivity assumptions

- Target GDP growth using a sector-specific TFP shifter subject to two contraints:
  - Agricultural productivity follows exogenous trajectories
  - A constant TFP growth wedge (2 p.p.) maintained between Industry and Services

# Efficiency assumptions

- Autonomous energy efficiency improvement
  - Region-specific coefficient, targets EconMap energy productivity improvements
  - No improvement in fossil energy production sectors
- Iceberg trade cost
  - None by default
  - (Optional) 25% reduction per 30 years calibrated to match past trade-to-income elasticities in the past
- TFP in the transportation sector
  - None by default
  - (Optional) 2% annual (i.e. same as industry) calibrated to match past trade-to-income elasticities in the past
- Agricultural yields, feed efficiency, emission rates
  - None.





## Consumer preferences

 None (excepted the convergence to a CES with the increase in income per capita)



# Input/output relations

■ No specific assumption.

### Energy mix

 No specific assumption (excepted endougenous adjustments to fossil energy prices).



Power sector

■ Treated as other sectors (extension under development).

# Future activities/commodities

None.

## Reporting

- Use of Fisher price index and volume index at initial prices for all aggregated indices
- Real income
  - Equivalent variation
  - Decomposition between allocation efficiency, capital accumulation, land supply, terms of trade, trade cost, variety and other gains (to be updated)